

Systemic Analysis of Singaporean Traffic Resilience through Epidemic Model

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- **Background**
- Introduction
 - SIR model
 - Network SIR
 - Percolation
- Propagative recovery
- 2-Type model
- Conclusion
 - Overview
 - Final thoughts

Background

- Traffic congestion used to be studied as a localized problem.
- Systemic level study of congestions in the **network spreading approach** provides new perspectives
 - Predictable
 - Explainable
 - Extrapolate
 - Dynamical model

Li, Daqing, et al. "Percolation transition in dynamical traffic network with evolving critical bottlenecks." Proceedings of the National Academy of Sciences 112.3 (2015): 669-672.

Saberi, Meead, et al. "A simple contagion process describes spreading of traffic jams in urban networks." Nature communications 11.1 (2020): 1616.

SIR model (fully mixed)

Predict the time evolution of spreading epidemic with a set of PDEs of S, I and R

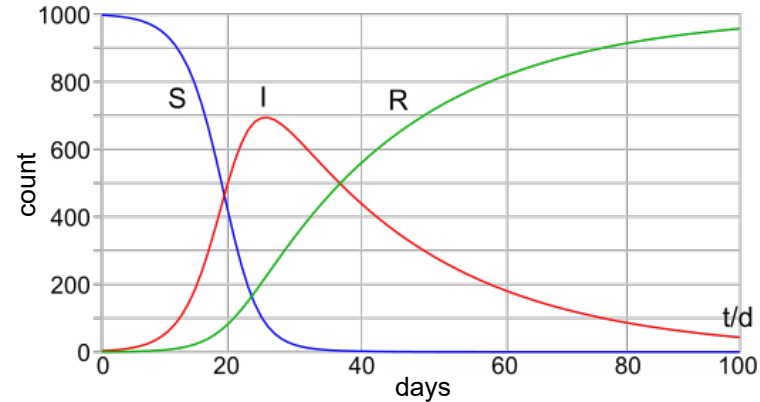
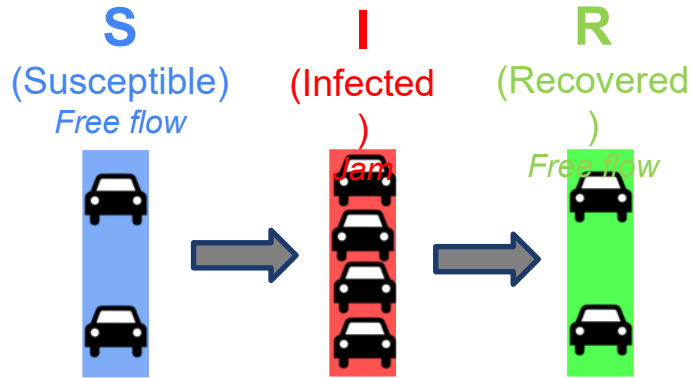
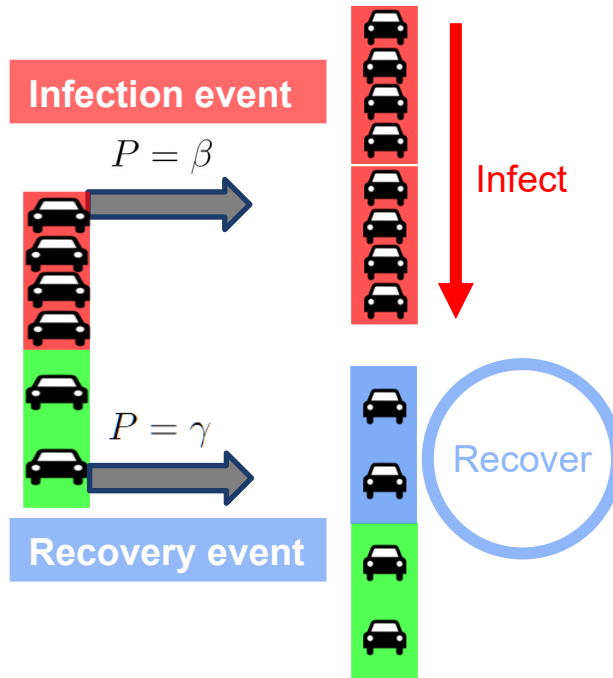


Diagram of the SIR-Model with $\beta = 0.0004$ and $\gamma = 0.04$. credit: Klaus-Dieter Keller, CC-BY

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Network SIR model



Network model keeps certain **mesoscopic** details:

- Respect the network structure
- Can describe geographical changes

Ignores certain **microscopic** details

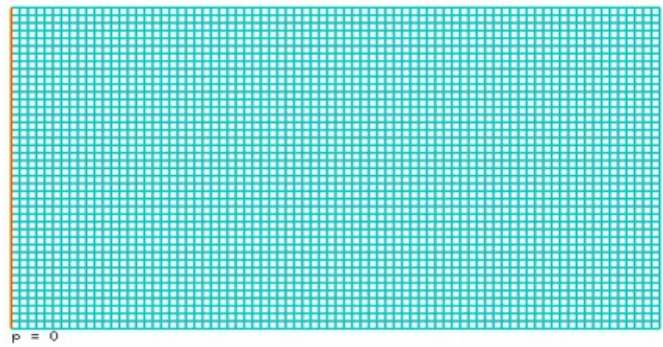
- Vehicle to vehicle/lane interactions
- Road width and geometries
- ...

β : probability for the disease to spread to a neighbour
 γ : probability to recover from infection

Percolation on network & phase transition

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- Percolation process: roads are infected (jammed) with probability p .
- Small p : many small infected/jammed components – little systemic impact
- Large p : one giant infected/jammed component – huge systemic impact.
- Small $p \rightarrow$ large p : percolation **phase transition** at critical threshold p_c .



Percolation on a square lattice visualized. Phase transition happens at $p=0.5$. credit: Nils Berglund, CC-BY https://www.youtube.com/watch?v=cl_B9iqsB9E

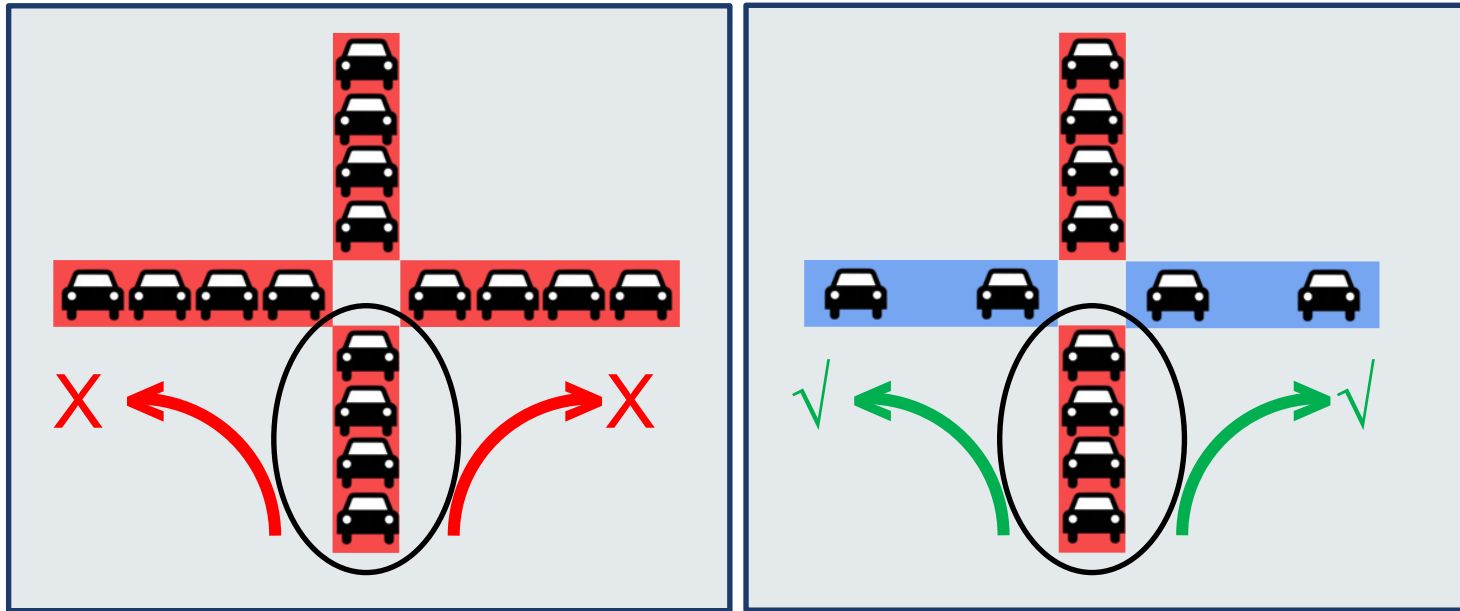
SIR process on Network is essentially a percolation process.



Zeng, G., et al. (2020). Multiple metastable network states in urban traffic. PNAS, 117(30), 17528-17534.

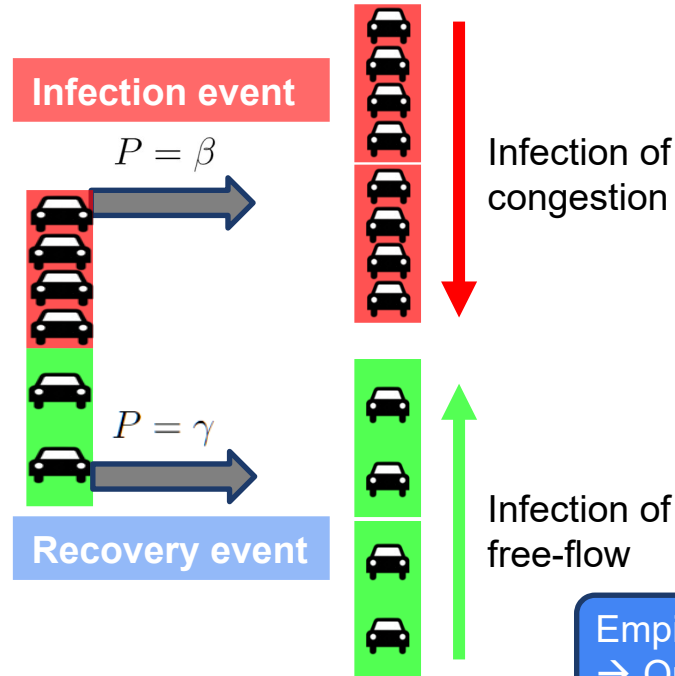
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Recovery is not spontaneous



The circled road on the right should recover more easily.
→ The recovery probability is dependent on the adjacent roads.

2-Type model and fitting result



2 types of disease: infection & congestion

Singaporean data shows:
Changing probability
= spreading + spontaneous

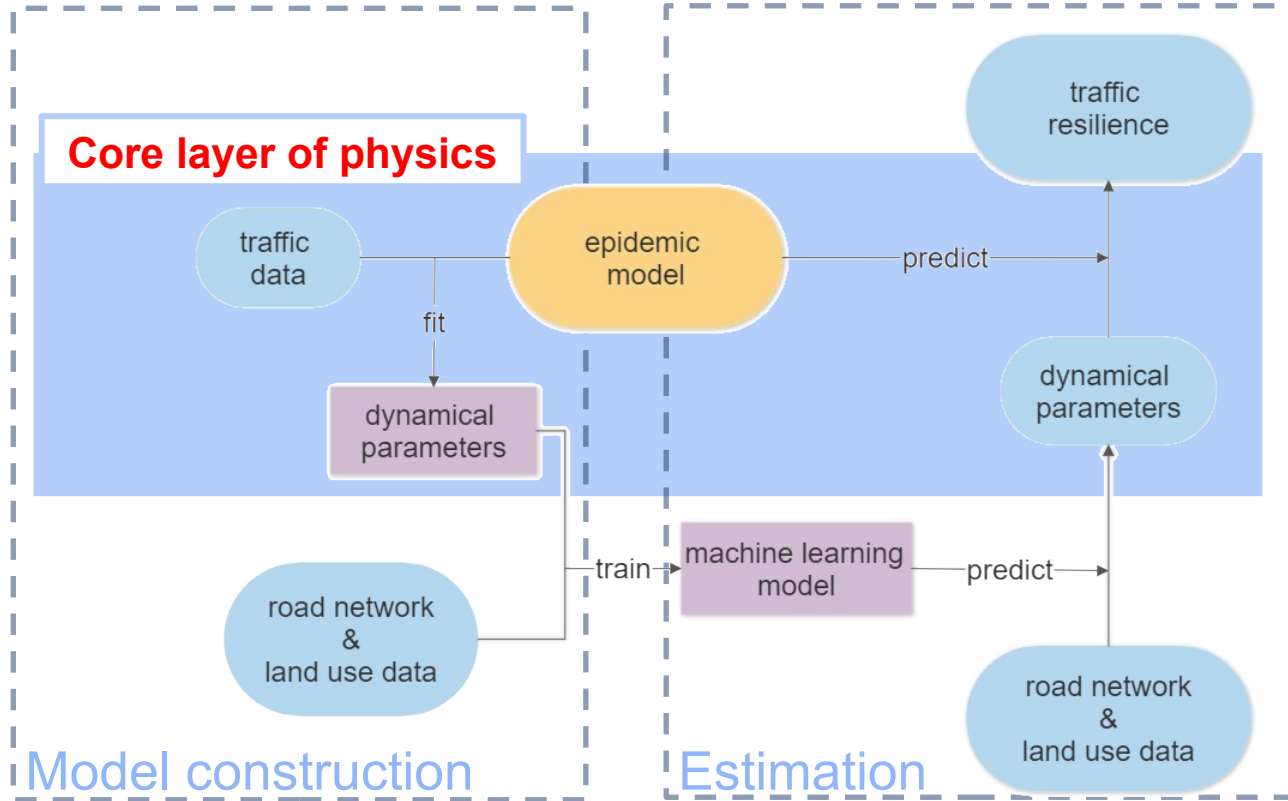
$$P(I|k_{\text{out}}, k_{\text{out},I}, \beta_I) \approx \underbrace{1 - (1 - \beta_I)^{k_{\text{out},I}}}_{\text{spreading}} + \underbrace{p_0}_{\text{spontaneous}}$$

$$p_{SG} = 0.285 \ll p_c \approx 0.4$$

Empirical p in SG is lower than the percolation threshold
→ Only small localized congestion possible

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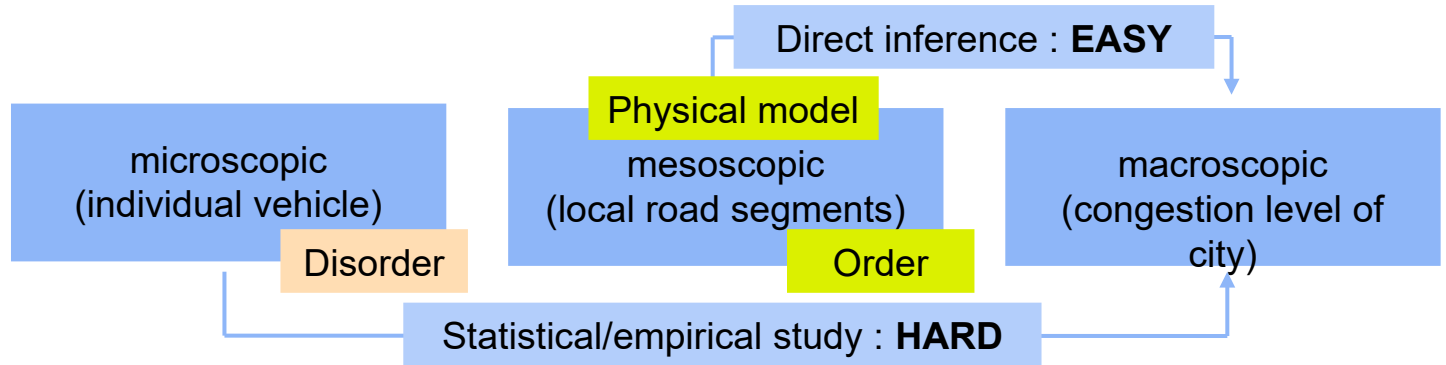
How could this model help urban design?



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Final thoughts – Look through scales for order

One way to understand an **emergent phenomenon**:



<https://pixabay.com/photos/highway-traffic-germany-streets-2909336/>



<https://pixabay.com/photos/long-exposure-cars-highway-traffic-1232709/>

Thank you