

# Long-term solar PV planning in High-Density Urban Systems

**URBAN SOLUTIONS  
AND SUSTAINABILITY**  
R&D CONGRESS 2023

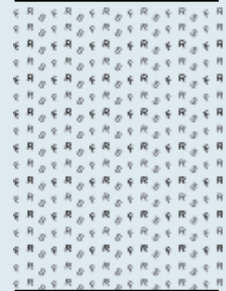
BUILDING SUSTAINABLE, RESILIENT, AND LIVABLE CITIES OF TOMORROW

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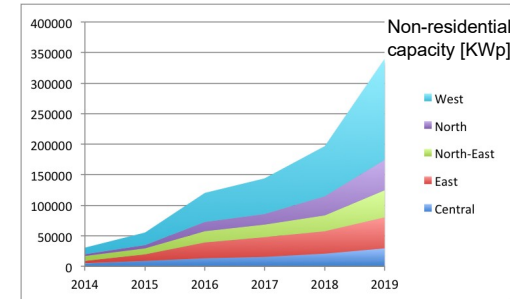
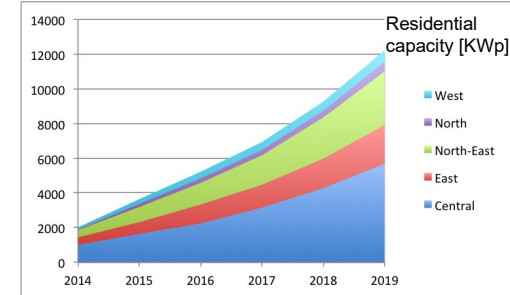
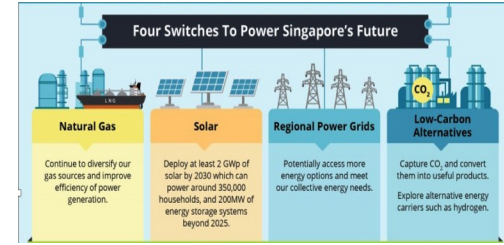
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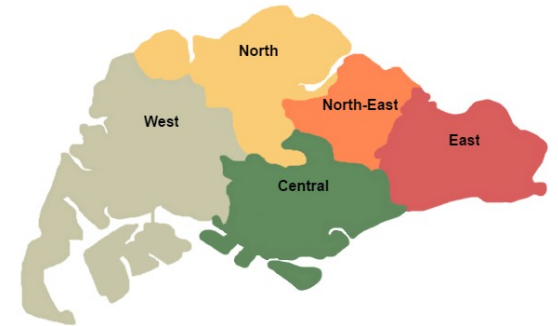
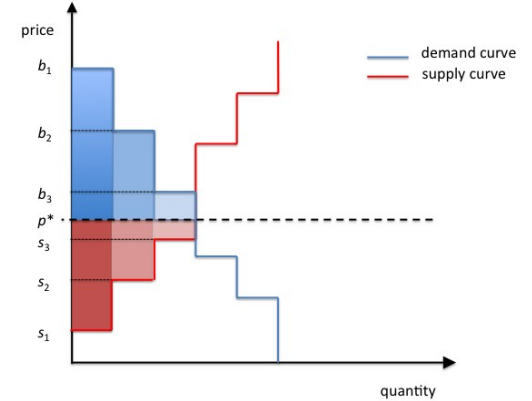
# Solar planning model: overview and motivation

- Singapore has very ambitious **solar capacity targets**
- The main sources of solar energy are rooftop/façade panels, but **space is scarce** and **consumers may be risk averse**
- How can **government/agencies** achieve targets?
- Our approach: robust optimization to **estimate solar adoption**
- Idea: after calibrating our model with past data, determine the **incentives** necessary to achieve the targets
- **Space availability** is considered as a constraint.



# Assumptions

- Decision of installing capacity depends on the **economic surplus principle** involving producers and consumers of solar PV (PhotoVoltaic) systems
- Test case: **Singapore, 2020-2050**
- **Limited** rooftop and façade **space**
- **Risk-averse** behaviour of consumers (robust optimization)
- Parameters to be **calibrated**: net space used, maximum buying price from consumers, budget of uncertainty.
- Requirement: meet **capacity targets** from government/agencies.



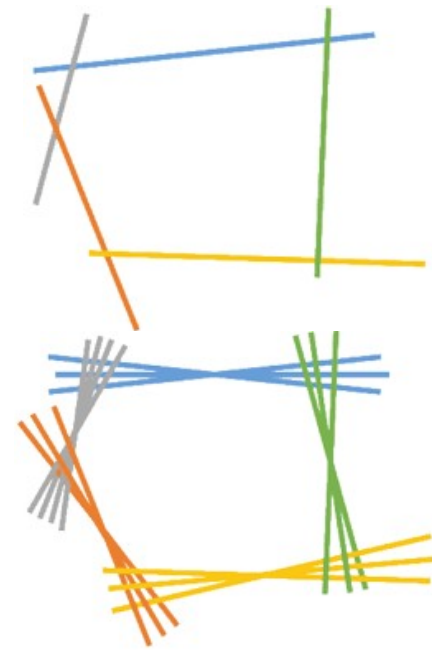
# Methodology: main idea

## 1. Robust optimization model:

- Objective: maximization of the total economic surplus of buyers/sellers of solar PV systems
- Constraints: space availability, equilibrium of capacity bought/sold
- Uncertainty: maximum buying price; risk-averse consumers

## 2. Derivation and solution of the Robust Counterpart (linear program) to forecast capacity installed (2020-2050)

## 3. Analysis of the solution to derive incentives necessary to achieve capacity targets.



# Methodology: formulations

$$\begin{aligned}
 \max \quad & \left( \sum_{t \in T} -\beta_t \sum_{q \in Q} \sum_{k \in K_q} r_{t,k,q} w_{t,k,q} + \right. \\
 & \left. + \min_{\epsilon \in U(\Gamma)} \sum_{t \in T} \beta_t \sum_{l \in L} \sum_{c \in C} \sum_{k \in K} y_{l,t,k,c} \bar{p}_{l,t,k,c} (1 - \epsilon_{l,t,k,c}) \right) \\
 \text{s.t.} \quad & \forall t \in T, \forall k \in K \quad \sum_{l \in L} \sum_{c \in C} y_{l,t,k,c} = \sum_{q \in Q: k \in K_q} w_{t,k,q} \\
 & \forall l \in L, \forall t \in T, \forall c \in C, \forall j \in J \quad s_{l,t,c,j} = \sum_{k \in K_j} \frac{y_{l,t,k,c}}{\eta_{k,t}} \\
 & \forall l \in L, \forall t \in T, \forall c \in C, \forall j \in J \quad \sum_{t' \in T: t' \leq t} s_{l,t',c,j} \leq \sum_{t' \in T: t' \leq t} a_{l,t',c,j} \\
 & \mathbf{y}, \mathbf{w}, \mathbf{s} \geq \mathbf{0}.
 \end{aligned}$$

uncertainty (risk-averse consumers)

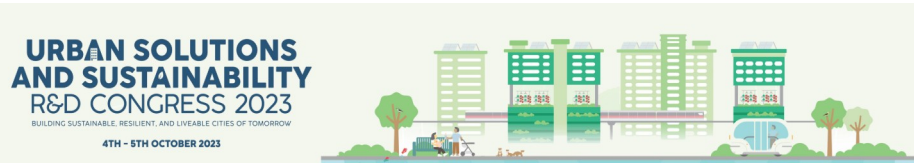


$$\begin{aligned}
 \max \quad & \sum_{t \in T} \beta_t \left( \sum_{l \in L} \sum_{c \in C} \sum_{k \in K} \bar{p}_{l,t,k,c} y_{l,t,k,c} - \sum_{q \in Q} \sum_{k \in K_q} r_{t,k,q} w_{t,k,q} \right) + \\
 & + \sum_{l \in L} \sum_{c \in C} \rho_{l,c} \Gamma_{l,c} + \sum_{l \in L} \sum_{t \in T} \sum_{k \in K} \sum_{c \in C} \mu_{l,t,k,c} \\
 \text{s.t.} \quad & \forall t \in T, \forall k \in K \quad \sum_{l \in L} \sum_{c \in C} y_{l,t,k,c} = \sum_{q \in Q: k \in K_q} w_{t,k,q} \\
 & \forall l \in L, \forall t \in T, \forall c \in C, \forall j \in J \quad s_{l,t,c,j} = \sum_{k \in K_j} \frac{y_{l,t,k,c}}{\eta_{k,t}} \\
 & \forall l \in L, \forall t \in T, \forall c \in C, \forall j \in J \quad \sum_{t' \in T: t' \leq t} s_{l,t',c,j} \leq \sum_{t' \in T: t' \leq t} a_{l,t',c,j} \\
 & \forall l \in L, \forall t \in T, \forall k \in K, \forall c \in C \quad \rho_{l,c} + \mu_{l,t,k,c} + \beta_t y_{l,t,k,c} \bar{p}_{l,t,k,c} \leq 0 \\
 & \forall \tau \in \Omega \quad \sum_{l \in L} \sum_{k \in K} \sum_{c \in C} \sum_{t \in T: t \leq \tau} y_{l,t,k,c} \geq \psi_\tau \\
 & \mathbf{y}, \mathbf{w}, \mathbf{s} \geq \mathbf{0} \\
 & \rho, \mu \leq 0.
 \end{aligned}$$

target constraints

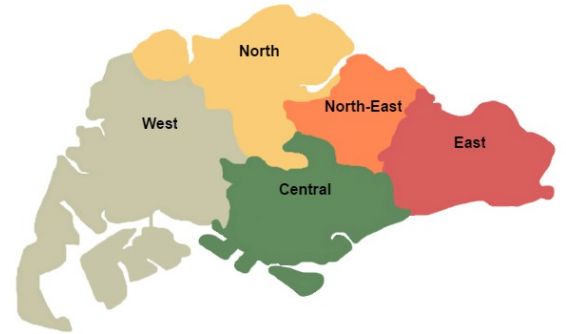
Robust optimization model

Robust counterpart (Linear Program)



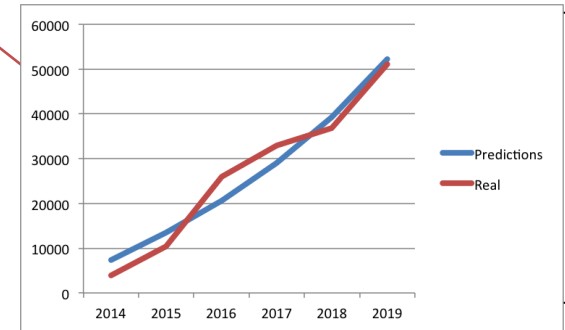
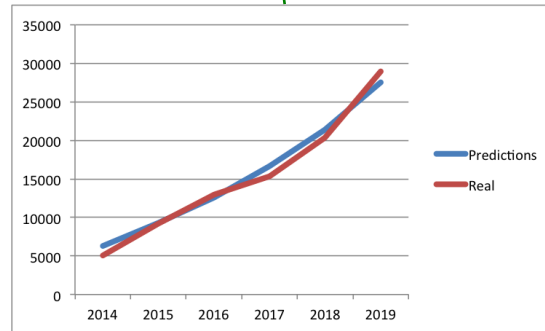
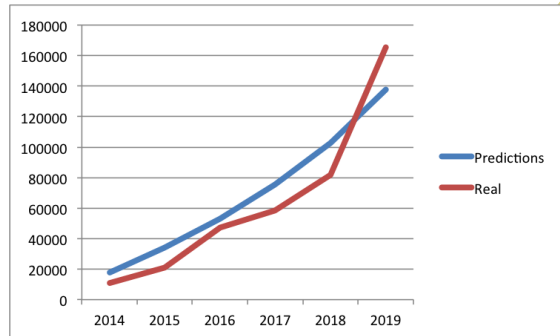
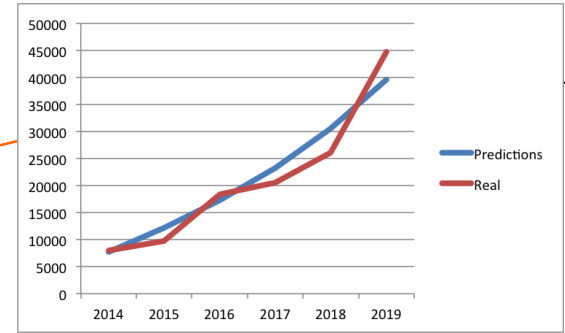
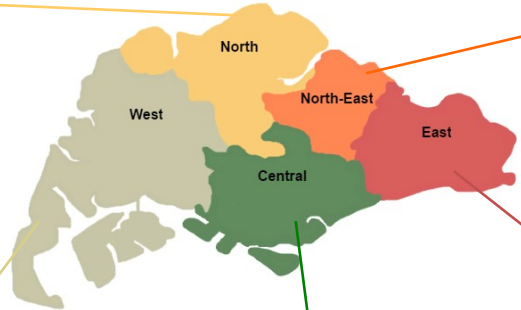
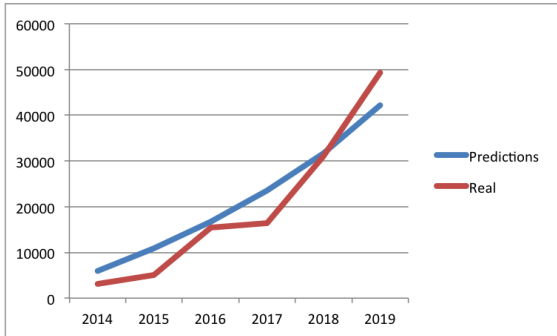
# Test case: background

- **Singapore** used as a case study for its potential in terms of solar energy
- **Rooftop**: for each region, 3 consumers: Residential, Commercial, Industrial
- **Façade**: single profile, no past data available
- **Data sources**: EMA, SERIS reports 2014/2020. Calibration for the other parameters of interest (net space used, maximum buying price from consumers, budget of uncertainty).



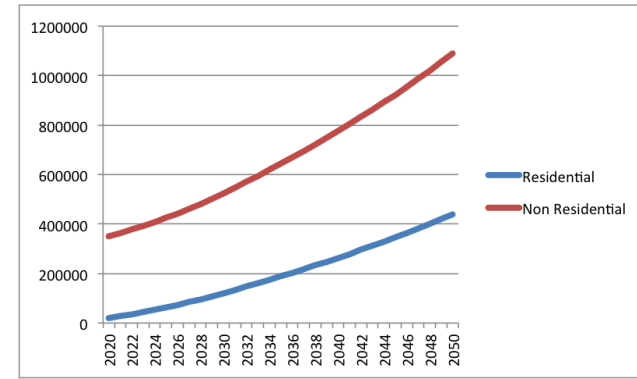
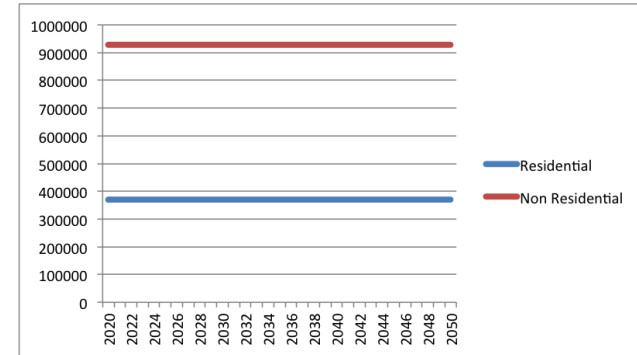
# Test case: calibration

- Singapore, 5 regions, residential/non-residential consumers
- Calibration: 2014-2018 capacity [KWp]. Validation: 2019



# Test case: the importance of uncertainty

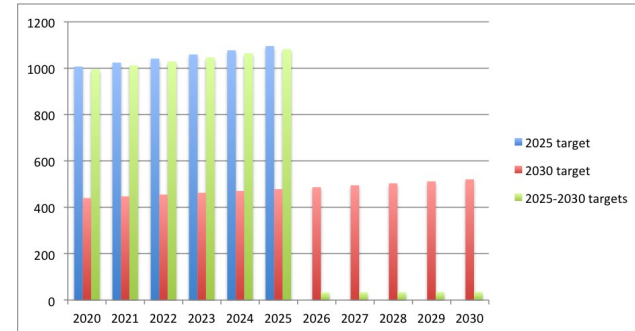
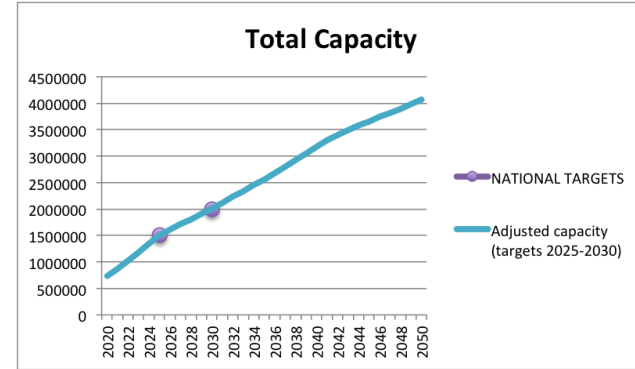
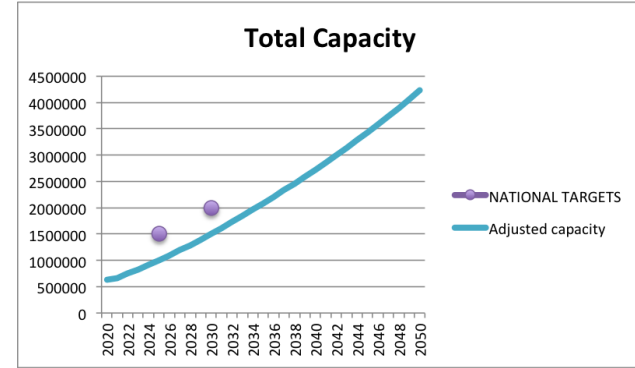
- Without including risk-aversion of buyers, results of the **deterministic model** show that rooftop capacity [KWp] is installed at the first time period (**unrealistic**)
- The **robust model** including risk-aversion of buyers produces more **meaningful results**.





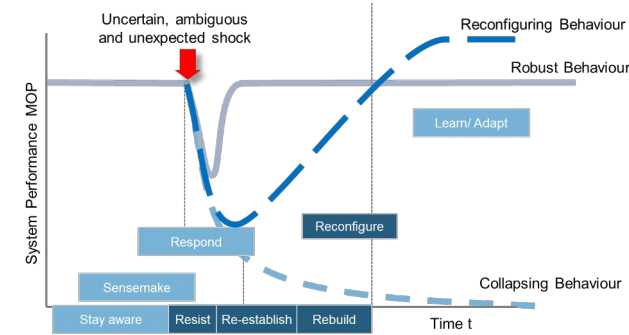
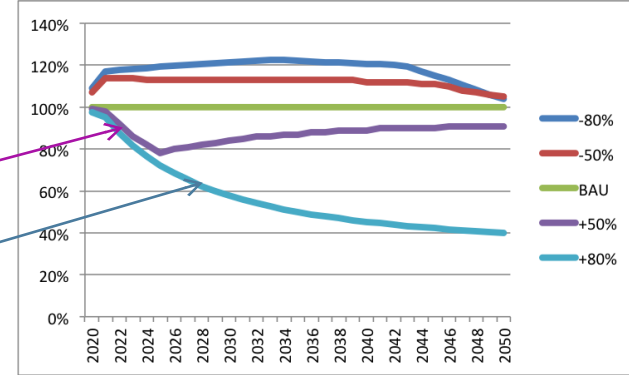
# Test case: total capacity and incentives

- **Model forecasting** (rooftop residential + non-residential and façade, all 5 regions capacity [KWp]) compared with national targets
- Without incentives, the targets in 2025 and 2030 **may not be achieved**
- Incentives to achieve targets [SGD/KWp] can be **derived directly** (dual variables of the target constraints).

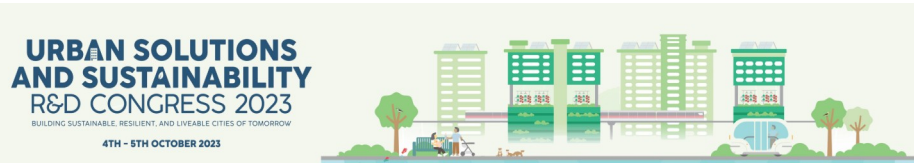


# Test case: resilience

- Effect of change of selling prices (shock event) on the capacity installed
- +50%: robust behaviour
- +80%: collapsing behaviour.

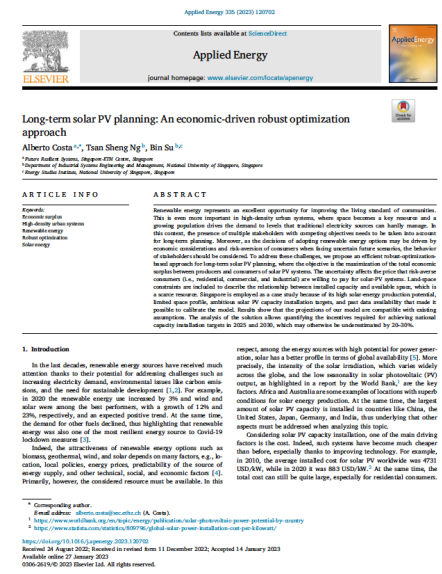


Credit: Hans R. Heinemann, 2019



# Conclusions

- Robust solar planning model including space constraints and risk-averse consumers yielding a linear programming problem
- This model can complement the analysis by agencies when deriving effective policies to address the conflicting objectives at a national level
- Reference: A. Costa, T.S. Ng, B. Su. Long-term solar PV planning: An economic-driven robust optimization approach. Applied Energy 335:120702. Elsevier, 2023.



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